

Demostreu que la corba  $y = x \sin x$  és tangent a la recta  $y = x$  quan  $\sin x = 1$ . I és tangent a la recta  $y = -x$  quan  $\sin x = -1$

Solució:

a)

$$\sin x = 1 \text{ quan } x = \frac{\pi}{2} + 2\pi k, \quad k \in \mathbb{Z}$$

Siga  $f(x) = x \sin x$

$$f\left(\frac{\pi}{2} + 2\pi k\right) = \left(\frac{\pi}{2} + 2\pi k\right) \sin\left(\frac{\pi}{2} + 2\pi k\right) = \frac{\pi}{2} + 2\pi k$$

$$f'(x) = \sin x + x \cos x.$$

El pendent de la corba quan  $x = \frac{\pi}{2} + 2\pi k, \quad k \in \mathbb{Z}$  és:

$$f'\left(\frac{\pi}{2} + 2\pi k\right) = \sin\left(\frac{\pi}{2} + 2\pi k\right) + \left(\frac{\pi}{2} + 2\pi k\right) \cos\left(\frac{\pi}{2} + 2\pi k\right) = 1 + 0 = 1$$

L'equació de la recta tangent quan  $x = \frac{\pi}{2} + 2\pi k, \quad k \in \mathbb{Z}$

$$r_T \equiv y - \left(\frac{\pi}{2} + 2\pi k\right) = 1 \left(x - \left(\frac{\pi}{2} + 2\pi k\right)\right)$$

Simplificant:

$$r_T \equiv y = x$$

b)

$$\sin x = -1 \text{ quan } x = \frac{3\pi}{2} + 2\pi k, \quad k \in \mathbb{Z}$$

$$f\left(\frac{3\pi}{2} + 2\pi k\right) = \left(\frac{3\pi}{2} + 2\pi k\right) \sin\left(\frac{3\pi}{2} + 2\pi k\right) = -\left(\frac{3\pi}{2} + 2\pi k\right)$$

El pendent de la corba quan  $x = \frac{3\pi}{2} + 2\pi k, \quad k \in \mathbb{Z}$  és:

$$f'\left(\frac{3\pi}{2} + 2\pi k\right) = \sin\left(\frac{3\pi}{2} + 2\pi k\right) + \left(\frac{3\pi}{2} + 2\pi k\right) \cos\left(\frac{3\pi}{2} + 2\pi k\right) = -1 + 0 = -1$$

L'equació de la recta tangent quan  $x = \frac{3\pi}{2} + 2\pi k, \quad k \in \mathbb{Z}$

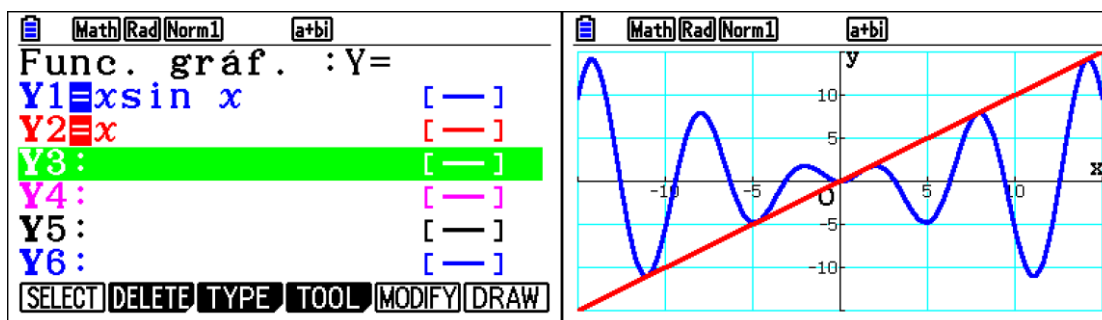
$$r_T \equiv y + \left(\frac{3\pi}{2} + 2\pi k\right) = -1 \left(x - \left(\frac{3\pi}{2} + 2\pi k\right)\right)$$

Simplificant:

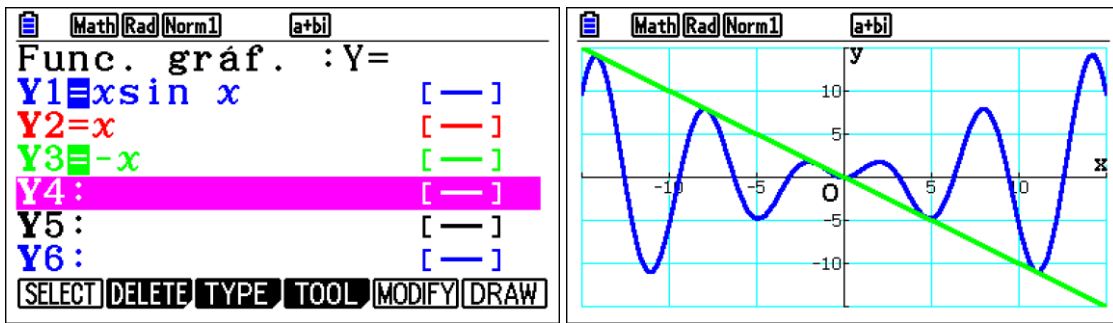
$$s_T \equiv y = -x$$

Obrim el *Menú Gráfico*.

Definim i representem  $f(x) = x \sin x$  i  $r_T \equiv y = x$



Definim i representem  $f(x) = x \sin x$  i  $s_T \equiv y = -x$



Ampliem la gràfica de les funcions al voltant de  $x = \frac{\pi}{2}$

